

Cluster IV

Data Analysis, Probability, and Discrete Mathematics

Probability

When we say that one event is more probable than another, we mean it is more likely to happen. If a person tosses a coin, there are only two ways it can fall—heads or tails. The coin is as likely to fall one way as the other. Thus the probability of getting a head is $\frac{1}{2}$ (theoretical probability). If a coin is tossed 100 times and x is the number of times heads occurs, we can expect the ratio $\frac{x}{100}$ to be close to $\frac{1}{2}$ (experimental probability).

Definitions:

Experimental probability is the probability of an event based on the result of an experiment.

Theoretical probability is the expected probability.

The probability that an event will occur is somewhere between 0 and 1.

A probability of 0 means that it is impossible for an event to occur.

Example 1. There are 12 blue and 6 red marbles in a bag. What is the probability of picking a yellow marble from the bag?

Solution: $P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{total number of possible outcomes}}$; $P(\text{yellow}) = \frac{0}{18} = 0$

A probability between 0 and 1 means that an event is possible.

Example 2. In example 1, what is the probability of picking a blue marble?

Solution: $P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{total number of possible outcomes}}$; $P(\text{blue}) = \frac{12}{18} = \frac{2}{3} = 0.67$